
Second-best Congestion Pricing Schemes in the Monocentric City

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Second-best congestion pricing

- Until recently: theoretical curiosity, but standard in practice
 - Cordon charge
 - Pay-lanes
 - Area charging
 - Parking policies
- Recently an upsurge in theoretical work
 - Often partial equilibrium (network) models
 - General equilibrium: labour market (Mayeres-Proost, Parry-Bento)
 - Urban spatial equilibrium models: focus on first-best pricing (second-best capacity); exceptions are Sullivan (1983) and Mun, Kunishi & Yoshikawa (2003)

Mun et al. (2003)

- Monocentric model, spaceless CBD, single radial road, place-dependent per-unit-of-distance (p.u.d.) congestion cost function
 - First-best: space-varying p.u.d. tolls
 - Surprising result: a single cordon (optimal location, 2nd-best optimal toll) yields 94% of first-best gains
 - Despite inherent weaknesses of the policy:
 - No charge for residents inside the cordon
 - Charge $>$ mec for residents outside but close to cordon
 - Charge $<$ mec for residents outside cordon close to fringe

This paper...

- Endogenizing land markets
 - rent and urban density
- Endogenizing labour market
 - space-varying endogenous labour supply
- General spatial equilibrium
 - 3-way interactions between congestion, density, labour supply
- Two second-best congestion taxes
 - cordon charge
 - flat km charge

The model (1)

- The city is...
 - one-dimensional (z) of endogenous size (z^*)
 - closed (N)
 - The CBD...
 - is spaceless
 - hosts the city's single sector; perfect competition
 - Land rents...
 - are endogenous
 - with excess rents (above $z^* \times r_A$) lump-sum redistributed
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The model (2)

- Consumers...

- maximize a utility function with 3 arguments:
 - leisure (T_f)
 - space ($s=1/n$)
 - industrial goods (y)
 - under a financial gross budget constraint M
 - Specification of M assumes full time working; labour-leisure trade-off is modelled as if leisure is bought against net wage
 - under a time constraint
 - Total time $T = \text{leisure } (T_f) + \text{work } (T_w) + \text{commuting } (T_c)$
 - commuting time $T_c(z)$ is to be determined
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The model (3)

■ Travel time

- $T_c(z) = T_w(z) \times T_t(z)$
 - $T_t(z) =$ Integral of p.u.d. travel times $t(x)$ between CBD ($z=0$) and residential location (z)
 - $t(x)$, in turn, depends (through congestion) on cumulative labour supply between point x and the urban fringe (z^*)
 - Complicated interactions: labour supply at a certain location depends on travel times, and hence on labour supply at all other locations
 - No analytical solutions
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The model (4)

- Producers...
 - exogenous central location in spaceless CBD
 - linear production function with one input
 - labour
 - perfect competition drives profits to zero
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The model (5)

- Important equilibrium conditions
 - Balanced budgets for consumers and government; zero-profit for firms; trade balance
 - Utility maximizing consumption of y , s and T_f at each location
 - Resulting utility constant over space
 - Rent at urban fringe equal to agricultural rent
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The model (6)

- Equilibrium requires the solution of 19 equations in 19 unknowns, some of which are functions of location (z)
- Numerical approach
 - for Cobb-Douglas and CES utility
 - a linear p.u.d. travel time function
 - normalizations where possible ($T, p, r_A; N=1000$)
- Calibration: attempt to obtain reasonable key ratios
 - details in paper, but for example:
 - 26.5 hours of labour per 7-day working week
 - maximum travel time of 5 hours (return) per working day
 - equilibrium speed near CBD 20% of free-flow speed
 - financial budget shares: 43% on housing, 57% on other goods

Equilibrium *vs* optimum

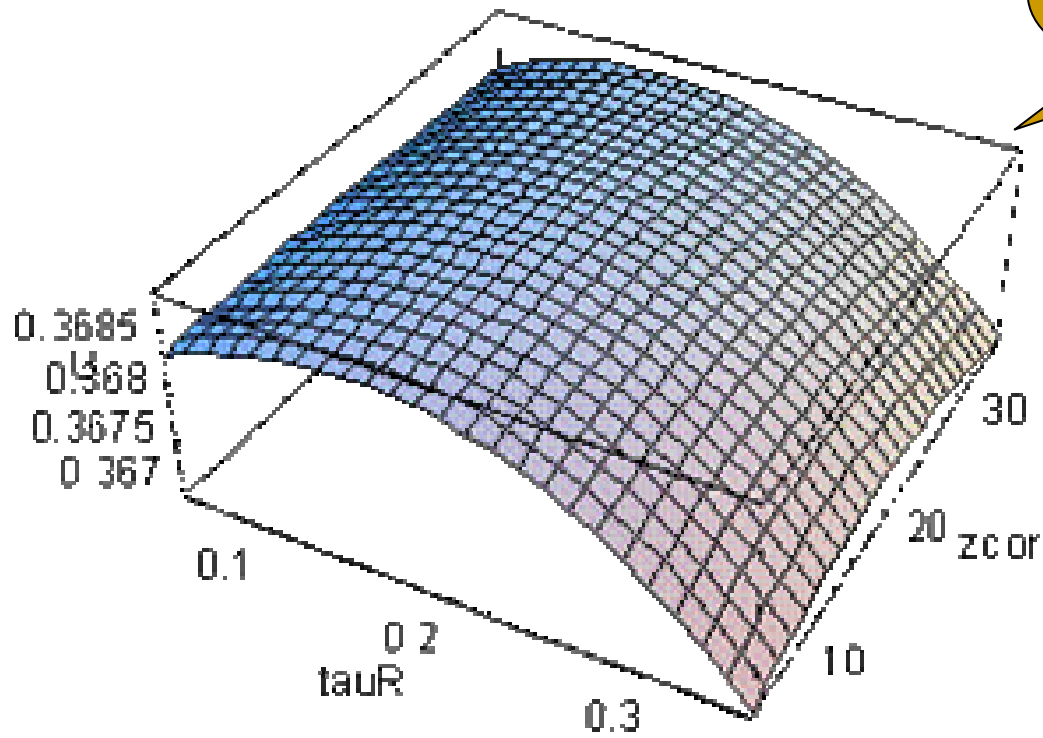
- Congestion entails externality
 - Optimum requires
 - Space-varying p.u.d. Pigouvian congestion taxes
 - Lump-sum recycling of the revenues
 - Main effects in numerical model:
 - Aggregate labour supply decreases with 6.6%
 - Average density increases: city size decreases 9.7%
 - Total kilometrage decreases by 16.9%
 - Total time spent commuting decreases by 21.2%
 - Utility increases by equivalent of 0.3% increase of each of the three consumption goods¹¹
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Sources of efficiency gains

- Two relevant margins of behaviour
 - Labour supply / employment
 - Space consumption / density
- Relative contribution: hard to disentangle, assessed by introducing inelasticities
 - Urban densities fixed: $\omega = 0.64$
 - Inelastic labour supply: $\omega = 0.48$
 - Not additive
 - Short run: nearly 2/3rds of long-run efficiency gains

Cordon charging

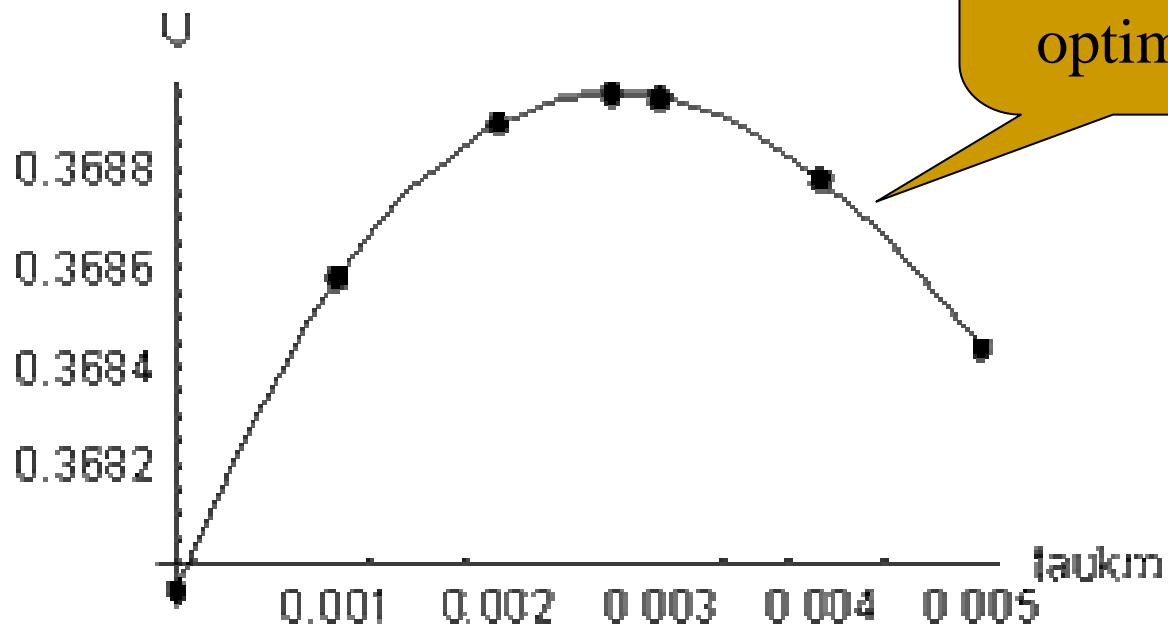
- Objective: optimize location and toll



Flat near optimum
More sensitive
wrt price than
location

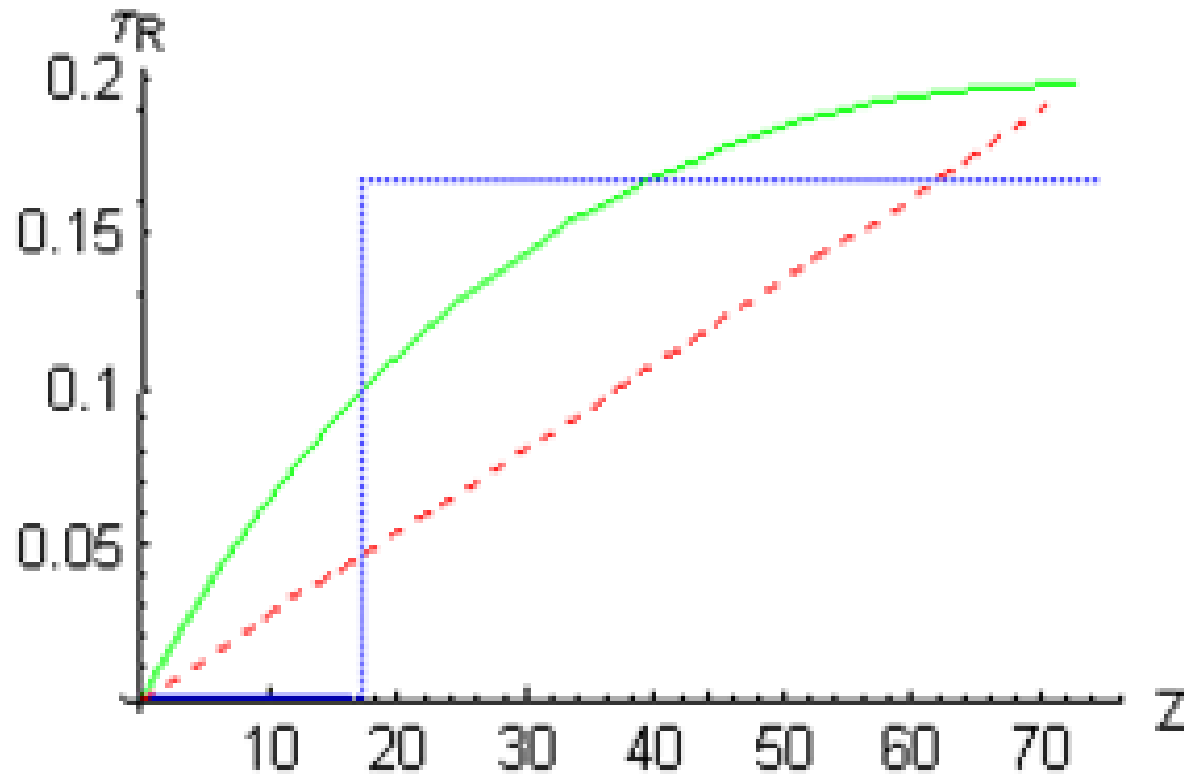
Flat km charge

- Objective: optimize flat toll level

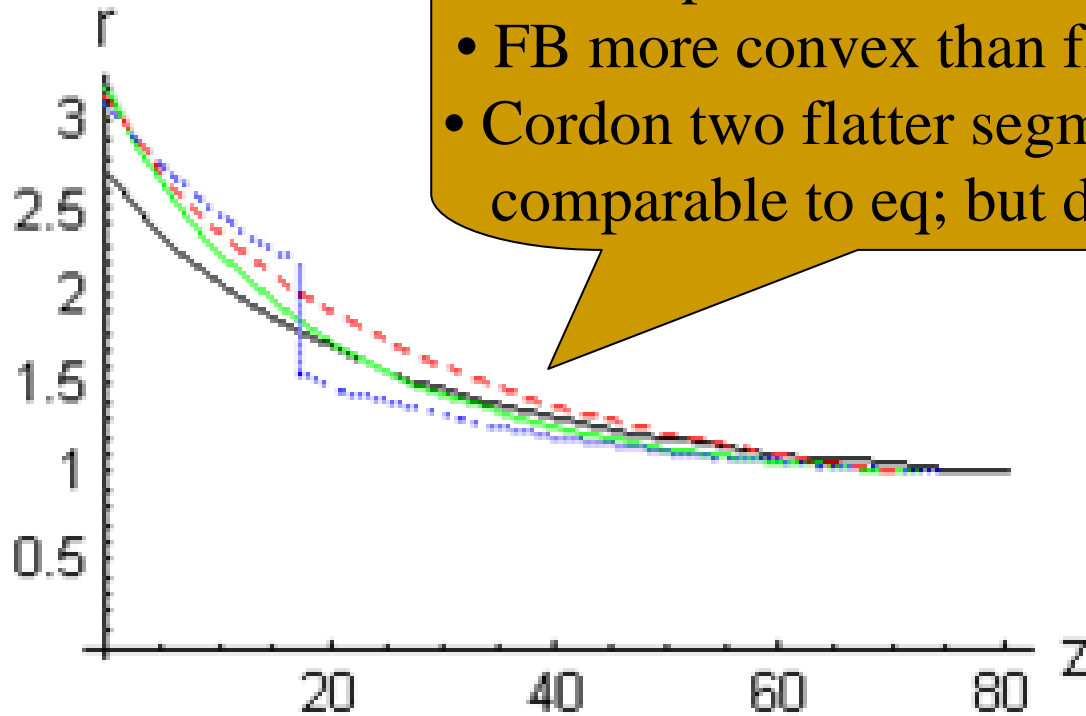


Flat near
second-best
optimum

Full-trip tolls

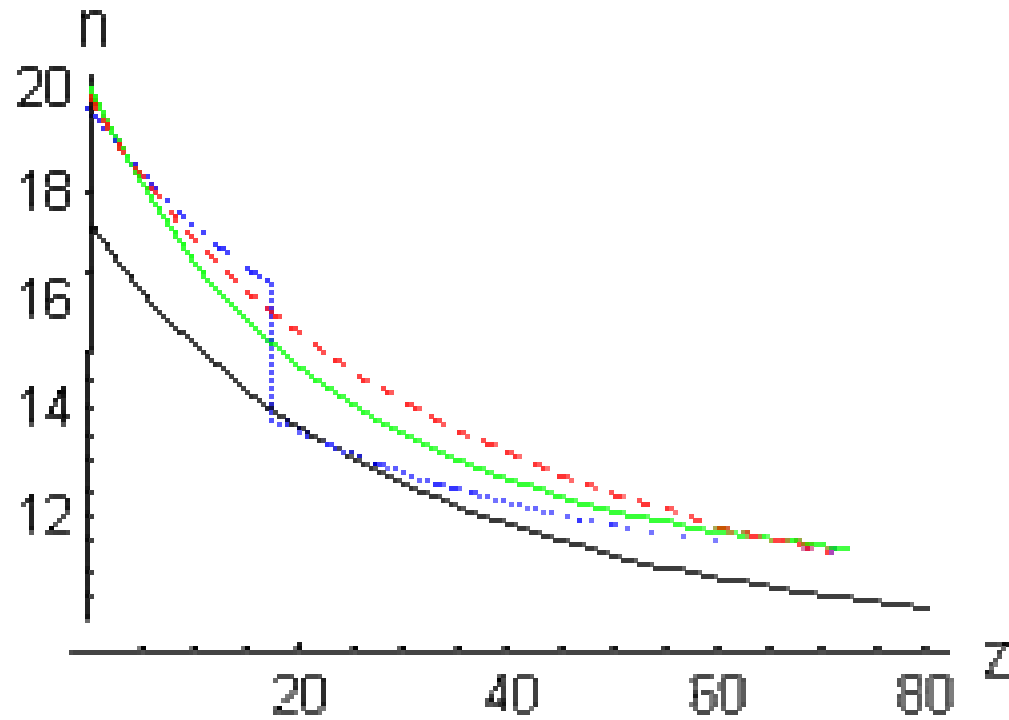


Rents



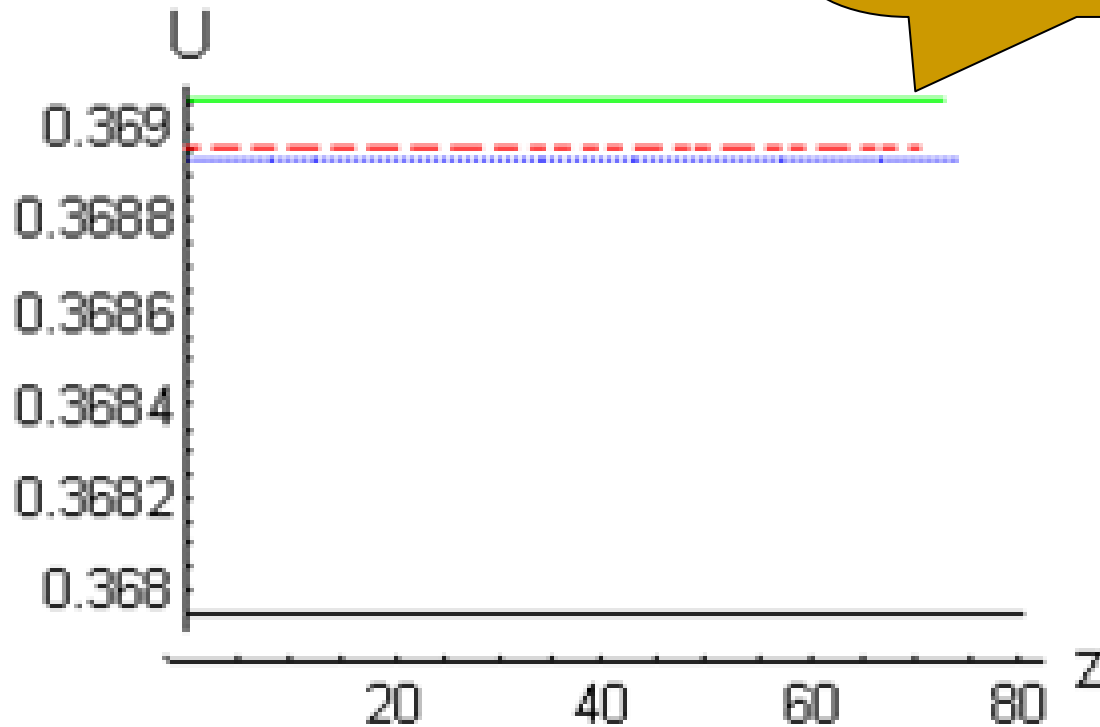
- FB steeper and more convex than eq.
- FB more convex than flat km charge
- Cordon two flatter segments than FB, comparable to eq; but discontinuity

Urban density



Utility

- Constant over space
- FB gains: 0.30%
- ω cordon: 0.880
- ω flat km: 0.899



Comparison with earlier work

- Cordon $\omega=0.88$ close to Mun *et al.* ($\omega=0.94$)
 - Surely, welfare loss have doubled
 - Nevertheless, inefficiencies in urban land and labour markets are apparently relatively small
- Flat km $\omega=0.90$ way above Sullivan ($\omega=0.30$)
 - Main difference appears to be naïve investment rule in Sullivan
 - Local 'CBA'; ignores 'network effects' (i.e. upstream and downstream of point of evaluation)
 - But: effect so large?

CES results

- Elasticity of substitution = 0.5
- Otherwise calibrated to mimic Cobb-Douglas budget shares as closely as possible
- Relative efficiency results are very similar
 - ω cordon = 0.897
 - ω flat km = 0.911
- But relevant curves are typically flatter and less curved (more limited substitution)

Conclusion (1)

- Surprising result of Mun et al survives (to a large extent) when
 - endogenizing urban density and land rents
 - endogenizing labour supply
 - adopting general spatial equilibrium approach
 - for Cobb Douglas and CES utility functions
 - Cordon charging causes kinks & imperfections, but:
 - reduces aggregate labour supply
 - increases average density
 - Cordon charging is outperformed, but not by much, by flat km charging
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Conclusion (2)

- Strong suspicion:
 - Monocentric configuration with spaceless CBD, both imposed exogenously, are 'responsible'
 - Future work: test endogenous formation of 'spacious' agglomerations within urban area
 - First priority
 - Explore the impacts of pre-existing distortive labour taxes
 - First result: relative performance of cordon and flat km charging is reversed for sufficiently high labour tax
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